# Zero Voltage Switching Resonant Power Conversion 

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#### Abstract

The technique of zero voltage switching in modern power conversion is explored. Several ZVS topologies and applications, limitations of the ZVS technique, and a generalized design procedure are featured. Two design examples are presented: a 50 Watt DC/DC converter, and an off-line 300 Watt multiple output power supply. This topic concludes with a performance comparison of ZVS converters to their square wave counterparts, and a summary of typical applications.


## Introduction

Advances in resonant and quasi-resonant power conversion technology propose alternative solutions to a conflicting set of square wave conversion design goals; obtaining high efficiency operation at a high switching frequency from a high voltage source. Currently, the conventional approaches are by far, still in the production mainstream. However, an increasing challenge can be witnessed by the emerging resonant technologies, primarily due to their lossless switching merits. The intent of this presentation is to unravel the details of zero voltage switching via a comprehensive analysis of the timing intervals and relevant voltage and current waveforms.

The concept of quasi-resonant, "lossless" switching is not new, most noticeably patented by one individual [1] and publicized by another at various power conferences $[2,3]$. Numerous efforts focusing on zero current switching ensued, first perceived as the likely candidate for tomorrow's generation of high frequency power converters [4,5,6,7,8]. In theory, the onoff transitions occur at a time in the resonant cycle where the switch current is zero, facilitat-
ing zero current, hence zero power switching. And while true, two obvious concerns can impede the quest for high efficiency operation with high voltage inputs.

By nature of the resonant tank and zero current switching limitation, the peak switch current is significantly higher than its square wave counterpart. In fact, the peak of the full load switch current is a minimum of twice that of its square wave kin. In its off state, the switch returns to a blocking a high voltage every cycle. When activated by the next drive pulse, the MOSFET output capacitance ( $C_{\text {oss }}$ ) is discharged by the FET, contributing a significant power loss at high frequencies and high voltages. Instead, both of these losses are avoided by implementing a zero voltage switching technique [9,IO].

## Zero Voltage Switching Overview

Zero voltage switching can best be defined as conventional square wave power conversion during the switch's on-time with "resonant" switching transitions. For the most part, it can be considered as square wave power utilizing a constant off-time control which varies the conversion frequency, or on-time to maintain regulation of the output voltage. For a given unit of time, this method is similar to fixed frequency conversion which uses an adjustable duty cycle, as shown in Fig. 1.

Regulation of the output voltage is accomplished by adjusting the effective duty cycle, performed by varying the conversion frequency. This changes the effective on-time in a ZVS design. The foundation of this conversion is simply the volt-second product equating of the input and output. It is virtually identical to that of square wave power conversion, and vastly


Fig. 1 - Zero Voltage Switching vs. Conventional Square Wave
unlike the energy transfer system of its electrical dual, the zero current switched converter.

During the ZVS switch off-time, the L-C tank circuit resonates. This traverses the voltage across the switch from zero to its peak, and back down again to zero. At this point the switch can be reactivated, and lossless zero voltage switching facilitated. Since the output capacitance of the MOSFET switch ( $C_{\text {oss }}$ ) has been discharged by the resonant tank, it does not contribute to power loss or dissipation in the switch. Therefore, the MOSFET transition losses go to zero - regardless of operating frequency and input voltage. This could represent a significant savings in power, and result in a substantial improvement in efficiency. Obviously, this attribute makes zero voltage switching a suitable candidate for high frequency, high voltage converter designs. Additionally, the gate drive requirements are somewhat reduced in a ZVS design due to the lack of the gate to drain (Miller) charge, which is deleted when $V_{D S}$ equals zero.

The technique of zero voltage switching is applicable to all switching topologies; the buck regulator and its derivatives (forward, half and full bridge), the flyback, and boost converters, to name a few. This presentation will focus on the continuous output current, buck derived topologies, however a list of references describing the others has been included in the appendix.


Fig. 2-Resonant Switch Implementation


Fig. 3-General Waveforms

## ZVS Benefits

- Zero power "Lossless" switching transitions
- Reduced EMI / RFI at transitions
- No power loss due to discharging $C_{\text {oss }}$
- No higher peak currents, (ie. ZCS) same as square wave systems
- High efficiency with high voltage inputs at any frequency
- Can incorporate parasitic circuit and component $\boldsymbol{L} \boldsymbol{\&} \boldsymbol{C}$
- Reduced gate drive requirements (no "Miller" effects)
Short circuit tolerant


## ZVS Differences:

- Variable frequency operation (in general)
- Higher off-state voltages in single switch, unclamped topologies
$\square$ Relatively new technology - users must climb the learning curve
- Conversion frequency is inversely proportional to load current
- A more sophisticated control circuit may be required


## ZVS Design Equations

A zero voltage switched Buck regulator will be used to develop the design equations for the various voltages, currents and time intervals associated with each of the conversion periods which occur during one complete switching cycle. The circuit schematic, component references, and relevant polarities are shown in Fig. 4.

Typical design procedure guidelines and "shortcuts" will be employed during the analysis' for the purpose of brevity. At the onset, all components will be treated as though they were ideal which simplifies the generation of the basic equations and relationships. As this section progresses, losses and non-ideal characteristics of the components will be added to the formulas. The timing summary will expound upon the equations for a precise analysis.

Another valid assumption is that the output


Fig. 4- Zero Voltage Switched Buck Regulator
filter section consisting of output inductor $L_{.}$, and capacitor $\mathrm{C}_{0}$ has a time constant several orders of magnitude larger than any power conversion period. The filter inductance is large in comparison to that of the resonant inductor's value $L_{R}$ and the magnetizing current $\Delta I_{L o}$ as well as the inductor's DC resistance is negligible. In addition, both the input voltage $V_{I N}$ and output voltage $V_{o}$ are purely DC , and do not vary during a given conversion cycle. Last, the converter is operating in a closed loop configuration which regulates the output voltage $V_{o}$.

## Initial Conditions: Time interval $<\boldsymbol{t}_{\boldsymbol{0}}$

Before analyzing the individual time intervals, the initial conditions of the circuit must be defined. The analysis will begin with switch $Q_{1}$ on, conducting a drain current $I_{D}$ equal to the output current $\mathrm{I}_{0}$, and $V_{D S}=V_{C R}=0$ (ideal). In series with the switch $Q_{I}$ is the resonant inductor $L_{R}$ and the output inductor $L_{O}$ which also conduct the output current $I_{O}$. It has been established that the output inductance $L_{o}$ is large in comparison to the resonant inductor $L_{\boldsymbol{R}}$ and all components are ideal. Therefore, the voltage across the output inductor $V_{L o}$ equals the input to output voltage differential; $V_{L_{o}}=$ $V_{I N}-V_{0}$. The output filter section catch diode $\mathbf{D}_{0}$ is not conducting and sees a reverse voltage equal to the input voltage; $V_{D o}=V_{I}$, observing the polarity shown in Figure 4.

## Table I - INITIAL CONDITIONS

| COMP. | STATUS | CIRCUIT VALUES |
| :--- | :--- | :--- |
| $Q_{1}$ | ON | $V_{D S}=V_{C R}=0 ; I_{D}=I_{L R}=I_{L O}=I_{O}$ |
| $D_{O}$ | OFF | $V_{D O}=V_{I N} ; I_{D O}=0$ |
| $L_{R}$ |  | $I_{L R}=I_{O} ; V_{L R}=0$ |
| $L_{O}$ |  | $V_{L O}=V_{I N}-V_{O} ; I_{L O}=0$ |

## Capacitor Charging State: $\boldsymbol{t}_{\boldsymbol{0}}-\boldsymbol{t}_{\boldsymbol{I}}$

The conversion period is initiated at time $t_{0}$ when switch $Q_{I}$ is turned OFF. Since the current through resonant inductor $L_{R}$ and output inductor $L_{o}$ cannot change instantaneously, and no drain current flows in $Q_{1}$ while


Fig. 5 - Simplified M odel


Fig. 6 - Resonant Capacitor Waveforms
it is off, the current is diverted around the switch through the resonant capacitor $C_{R}$. The constant output current will linearly increase the voltage across the resonant capacitor until it reaches the input voltage $\left(V_{C R}=V_{I N}\right)$. Since the current is not changing, neither is the voltage across resonant inductor $L_{R}$.

At time $t_{0}$ the switch current $I_{D}$ "instantly" drops from $I_{O}$ to zero. Simultaneously, the resonant capacitor current $I_{C R}$ snaps from zero to I,, while the resonant inductor current $I_{L R}$ and output inductor current $I_{L O}$ are constant and also equal to $I_{o}$ during interval $t_{01}$. Voltage across output inductor $L_{O}$ and output catch diode $D_{o}$ linearly decreases during this interval due to the linearly increasing voltage across resonant capacitor $C_{R}$. At time $\boldsymbol{t}_{\boldsymbol{I}}, V_{C R}$ equals $V_{I N}$, and $D_{O}$ starts to conduct.

Table II - CAPACITOR CHARGING: $\mathbf{t}_{\mathbf{0}}-\mathbf{t}_{\mathbf{1}}$

| COMP. | Status | CIRCUIT VALUES |
| :---: | :---: | :---: |
| $\mathrm{Q}_{1}$ | OFF | $\mathrm{I}_{\mathrm{D}}=0 ; \mathrm{V}_{\mathrm{DS}(\mathrm{t})}=\mathrm{V}_{\text {CR(t) }}$ |
| $\mathrm{C}_{\text {R }}$ | Charging | $\mathrm{I}_{\mathrm{CR}}=0 ; \mathrm{V}_{\mathrm{CR}(\mathrm{t})}$ RISES LINEARLY $V_{C R(t 0)}=0 ; V_{C R(t 1)}=V_{I N}$ |
| $L_{R}$ |  | ${ }_{1 / R(t)}=I_{0} ; V_{\text {LR }}=0$ |
| $\mathrm{D}_{\mathrm{o}}$ | OFF | $\begin{gathered} V_{\text {DO(t) } 0}=V_{I N} ; V_{\text {DO(t) })}=0 ; \\ \text { DECREASES UNEARLY } \end{gathered}$ |
| Lo |  | $\begin{aligned} & V_{\text {LO(tO) }}=V_{I N}-V_{O} ; V_{\text {LO(t11 }}=-V_{O} \\ & \text { DECREASES LINEARLY; } I_{\text {LO }}=I_{0} \end{aligned}$ |

## Resonant State: $\mathbf{t}_{\mathbf{1}}-\mathbf{t}_{\mathbf{2}}$

The resonant portion of the conversion cycle begins at $t_{l}$ when the voltage across resonant capacitor $V_{C R}$ equals the input voltage $V_{I N}$, and the output catch diode begins conducting. At $\boldsymbol{t}_{\boldsymbol{I}}$, current through the resonant components $I_{C R}$ and $I_{L R}$ equals the output current $I_{O}$.

The stimulus for this series resonant L-C circuit is output current $I_{O}$ flowing through the resonant inductor prior to time $t_{l}$. The ensuing resonant tank current follows a cosine function beginning at time $\boldsymbol{t}_{l}$, and ending at time $\boldsymbol{t}_{2}$. At the natural resonant frequency $\omega_{\mathbf{R}}$, each of the L-C tank components exhibit an impedance equal to the tank impedance, $Z_{R}$. Therefore, the peak voltage across $C_{R}$ and switch $Q_{I}$ are a function of $Z_{R}$ and $I_{O}$.

The instantaneous voltage across $C_{R}$ and $Q_{l}$ can be evaluated over the resonant time interval using the following relationships:

$$
\begin{aligned}
& V_{C R(t)}=V_{C R(I)}+\frac{I_{o}}{\omega_{R} C_{R}} \sin \left[\omega_{R}\left(t-t_{1}\right)\right]_{t_{1}}^{2} \\
& Z_{R}=1 / \omega_{R} C_{R} \quad ; \quad V_{C R(I)}=V_{I N} \\
& \therefore \quad V_{C R(t)}=V_{I N}+I_{o} Z_{R} \sin \left[\omega_{R}\left(t-t_{1}\right)\right]_{t_{1}}^{2}
\end{aligned}
$$

Of greater importance is the ability to solve the equations for the precise off-time of the switch. This off-time will vary with line and load changes and the control circuit must respond in order to facilitate true zero voltage switching. While some allowance does exist for a fixed off time technique, the degree of lati-
tude is insufficient to accommodate typical input and output variations, The exact time is obtained by solving the resonant capacitor voltage equations for the condition when zero voltage is attained.

$$
\text { Let } V_{C R(t)}=0 ; I_{0} Z_{R} \operatorname{SIN}\left(\omega_{R}\left(t-t_{1}\right)\right)=-V_{I N}
$$

The equation can be further simplified by extracting the half cycle ( 180 degrees) of conduction which is a constant for a given resonant frequency, and equal to $\pi / \omega_{R}$.

$$
t_{12}=\frac{\pi}{\omega_{R}}+\frac{1}{\omega_{R}} \arcsin \left[\frac{V_{I N}}{I_{o} Z_{R}}\right]_{t_{1}}^{t_{2}}
$$

The resonant component current $\left(I_{C R}=I_{L R}\right)$ is a cosine function between time $\boldsymbol{t}_{1}$ and $t_{2}$, described as:

$$
I_{C R(t)}=I_{o} \cos \left[\omega_{R}\left(t-t_{1}\right)\right]_{t_{1}}^{t_{1}}
$$

The absolute maximum duration for this interval occurs when 270 degrees $\left(3 \pi / 2 \omega_{\mathbf{R}}\right)$ of resonant operation is required to intersect the zero voltage axis. This corresponds to the limit of resonance as minimum load and maximum line voltage are approached.

Contributions of line and load influences on the resonant time interval $t_{12}$ can be analyzed individually as shown in Figs. 7 and 8.

Prior to time $\boldsymbol{t}_{\boldsymbol{l}}$, the catch diode $\boldsymbol{D}_{\boldsymbol{o}}$ was not conducting. Its voltage, $V_{D O}$, was linearly decreasing from $V_{I N}$ at time $\boldsymbol{t}_{0}$ to zero at $\boldsymbol{t}_{1}$ while input source $V_{I N}$ was supplying full output current, $I_{0}$. At time $t_{l}$, however, this situation changes as the resonant capacitor initiates resonance, diverting the resonant inductor current away from the output filter section. Instantly, the output diode voltage, $V_{D 0}$, changes polarity as it begins to conduct, supplementing the decreasing resonant inductor current with diode current I', extracted from stored energy in output inductor $\boldsymbol{L}_{0}$. The diode current waveshape follows a cosine function during this interval, equalling $I_{0}$ minus $I_{C R}(\mathrm{t})$.

Also occurring at time $\boldsymbol{t}_{\boldsymbol{l}}$, the output filter inductor $L_{0}$ releases the stored energy required

t1L
Fig. 7 -- Resonant Capacitor Voltage vs. Line


Fig. 8 -- Resonant Capacitor Voltage vs. Load to maintain a constant output current $I_{o}$. Its reverse voltage is clamped to the output voltage $V_{0}$ minus the diode voltage drop $V_{D O}$ by the convention followed by Figure 4.
Table III - RESONANT INTERVAL: $\mathbf{t}_{\mathbf{1}} \cdot \mathbf{t}_{\mathbf{2}}$
COMP. STATUS
CIRCUIT VALUES

| $Q_{1}$ | OFF | $V_{D S(t)}=V_{C R(t)}$ |
| :---: | :---: | :---: |
| $\mathrm{C}_{\text {R }}$ | Resonant | $\begin{aligned} & V_{C R(t)}=V_{1 N}+\left(I_{0} Z_{R} \sin \left(\omega_{R}\left(t-t_{1}\right)\right)\right) \\ & I_{C R(t)}=I_{C} \cos \left(\omega_{R}\left(t-t_{1}\right)\right) \end{aligned}$ |
| $L_{R}$ | Resonant | $\begin{aligned} & V_{\operatorname{LR}(t)}=\left[l_{0} Z_{R} \sin \left(\omega_{R}\left(t-t_{1}\right)\right)\right. \\ & \operatorname{LRR}_{1(t)}=I_{C R(t)} \end{aligned}$ |
| $D_{0}$ | ON | $\mathrm{I}_{\mathrm{DO}(t)}=\mathrm{I}_{0}-\mathrm{L}_{\text {LR }}(t)$ |

## Inductor Charging State: $\boldsymbol{t}_{\mathbf{2}}-\boldsymbol{t}_{\mathbf{3}}$

To facilitate zero voltage switching, switch $Q_{1}$ is activated once the voltage $V_{D S}$ across $\boldsymbol{Q}_{1}$ and resonant capacitor $V_{C R}$ has reached zero, occurring at time $t_{2}$. During this inductor charging interval $t_{23}$ resonant inductor current $I_{L R}$ is linearly returned from its negative peak of minus $I_{O}$ to its positive level of plus $I_{O}$.

The output catch diode $D_{o}$ conducts during the $t_{23}$ interval. It continues to freewheel the full output current $I_{O}$, clamping one end of the resonant inductor to ground through $D_{o}$. There is a constant voltage, $V_{I N}-V_{D O}$, across the resonant inductor. As a result, $I_{L R}$ rises linearly, $I_{D O}$ decreases linearly. Energy stored in output inductor $L_{O}$ continues to be delivered to the load during this time period.

A noteworthy peculiarity during this timespan can be seen in the switch dram current waveform. At time $\boldsymbol{t}_{2}$, when the switch is turned on, current is actually returning from the resonant tank to the input source, $\boldsymbol{V}_{\text {IN }}$. This indicates the requirement for a reverse polarity diode across the switch to accommodate the bidirectional current. An interesting result is that the switch can be turned on at any time during the first half of the $t_{23}$ interval without affecting normal operation. A separate time interval could be used to identify this region if desired.

$$
\begin{gathered}
\frac{d I_{R}}{d t}=\frac{V_{I N}}{L_{R}} ; d t=d I_{R} L_{R} / V_{I N} \\
\therefore t_{23}=\frac{L_{R} \Delta I_{R}}{V_{I N}} \\
\text { where } \Delta I_{R}=-I_{O} \text { to }+I_{O}=2 I_{O} \\
t_{23}=\frac{2 L_{R} I_{O}}{V_{I N}} \text { and varies with } V_{I N} \text { and } V_{O}
\end{gathered}
$$

## Power Transfer State: $\boldsymbol{t}_{\mathbf{3}}-\boldsymbol{t}_{\mathbf{4}}$

Once the resonant inductor current $I_{L R}$ has reached $\boldsymbol{I}_{\boldsymbol{O}}$ at time $\boldsymbol{t}_{\mathbf{3}}$, the zero voltage switched converter resembles a conventional square wave power processor. During the remainder of

Table IV - INDUCTOR CHARGING: $\mathbf{t}_{\mathbf{2}} \cdot \mathbf{t}_{\mathbf{3}}$
COMP. STATUS CIRCUIT VALUES

| $Q_{1}$ | $O N$ | $\left.I_{D(t)}=-I_{0}+\left(V_{I N}+V_{D O}\right) / L_{R}\right) t$ |
| :--- | :--- | :--- |
| $C_{R}$ |  | $V_{C R}=0$ |
| $L_{R}$ | Charging | $V_{L R}=V_{I N}+V_{D O}$ |
|  |  | $I_{L R(t)}=-I_{O}+\left(V_{L R} / L_{R}\right)(t-t 2)$ |
| $D_{O}$ | $O N$ | $I_{D O(t)}=I_{0}-I_{L R(t)}$ |
| $L_{0}$ |  | $I_{L O}=I_{0} ; V_{L O}=-\left(V_{O}+V_{D O}\right)$ |

the conversion period, most of the pertinent waveforms approach DC conditions.

Assuming ideal components, with $Q_{1}$ closed, the input source supplies output current, and the output filter inductor voltage $V_{L O}$ equals $V_{I N}$ $-V_{o}$. The switch current and resonant inductor current are both equal to $I_{O}$, and their respective voltage drops are zero ( $V_{D S}=V_{L R}=0$ ). Catch diode voltage $V_{D O}$ equals $V_{I N}$, and $I_{D O}=0$.
In closed loop operation where the output voltage is in regulation, the control circuit essentially varies the on-time of the switch during the $t_{34}$ interval. Variable frequency operation is actually the result of modulating the on-time as dictated by line and load conditions. Increasing the time duration, or lowering the conversion frequency has the same effect as widening the duty cycle in a traditional square wave converter. For example, if the output voltage were to drop in response to an increased load, the conversion frequency would decrease in order to raise the effective ON period. Conversely, at light loads where little energy is drawn from the output capacitor, the control circuit would adjust to minimize the $t_{34}$ duration by increasing the conversion frequency. In summary, the conversion frequency is inversely proportional to the power delivered to the load.

$$
\begin{gathered}
V_{O}=\frac{V_{I N} t_{34}}{t_{01}+t_{12}+t_{23}+t_{34}}=\frac{V_{I N} t_{34}}{t_{03}+t_{34}} \\
t_{34}=\frac{V_{O} t_{03}}{V_{I N}-V_{O}}
\end{gathered}
$$

Table V-POWER TRANSFER: $\mathbf{t}_{3}-\mathbf{t}_{\mathbf{4}}$

| COMP. STATUS | CIRCUIT VALUES |  |
| :--- | :--- | :--- |
| $Q_{1}$ | $O N$ | $V_{D S}=I_{O} R_{D S(O N)} ; I_{D}=I_{O}$ |
| $C_{R}$ |  | $V_{C R}=0$ |
| $L_{R}$ |  | $I_{L R}=I_{O} ; V_{L R}=0$ |
| $D_{O}$ | OFF | $V_{D O}=V_{I N}$ |
| $L_{0}$ | Charging | $V_{L O}=V_{I N}-V_{O} ; I_{L O}=I_{0}$ |

$$
\begin{aligned}
V_{I N} & =18 \mathrm{~V} \\
V_{O} & =5 \mathrm{~V} \\
I_{O} & =5 \mathrm{~A}
\end{aligned}
$$



Fig. 9 -- ZVS Buck Regulator W aveforms

## ZVS Converter Limitations:

In a ZVS converter operating under ideal conditions, the on-time of the switch $\left(t_{23}+t_{34}\right)$ approaches zero, and the converter will operate at maximum frequency and deliver zero output voltage. In a practical design, however, the switch on-time cannot go to zero for several reasons.

First of all, the resonant tank components are selected based on the maximum input voltage $V_{\text {INmax }}$ and minimum output current $I_{\text {Omin }}$ for the circuit to remain resonant over all operating conditions of line and load. If the circuit is to remain zero voltage switched, then the resonant tank current cannot be allowed to go to zero. It can, however, reach $I_{O_{\text {min }}}$.

There is a finite switch on-time associated with the inductor charging interval $t_{23}$ where the resonant inductor current linearly increases from $-I_{o}$ to $+I_{O}$. As the on-time in the power transfer interval $t_{34}$ approaches zero, so will the converter output voltage. Therefore, the minimum on-time and the maximum conversion frequency can be calculated based upon the limitation of $\boldsymbol{I}_{\boldsymbol{O}_{\text {min }}}$ and zero output voltage.

The limits of the four zero voltage switched time intervals will be analyzed when $I_{o}$ goes to $I_{O}$ minimum. Each solution will be retained in terms of the resonant tank frequency $\omega_{R}$ for generalization.

$$
\begin{gathered}
C_{R}=\frac{1}{Z_{R} \omega_{R}}=\frac{I_{O_{\min }}}{V_{I N \max } \omega_{R}} \\
\therefore t_{01 \max }=\frac{C_{R} V_{I N \max }}{I_{O_{\min }}}=1 / \omega_{R} \\
t_{12 \max }=\frac{3 \pi}{2 \omega_{R}}=\frac{1.5 \pi}{\omega_{R}} \\
L_{R}=\frac{Z_{R}}{\omega_{R}}=\frac{V_{I N_{\max }}}{I_{O_{\min }} \omega_{R}}
\end{gathered}
$$

$$
\begin{gathered}
\therefore t_{23}=\frac{2 L_{R} I_{O \min }}{V_{I N \max }}=\frac{2}{\omega_{R}} \\
t_{34 \min }=0
\end{gathered}
$$

Both the minimum on-time and maximum off-time have been described in terms of the resonant tank frequency, $\omega_{\mathbf{R}}$. Taking this one step further will result in the maximum conversion frequency $f_{\text {CoNVmax }}$, also as a function of the resonant tank frequency.
Minimum On-Time:

$$
t_{23 \min }=\frac{2}{\omega_{R}}=\frac{1}{\pi f_{R}}=\frac{0.318}{f_{R}}
$$

## Maximum Off-Time:

$$
t_{01}+t_{12 \min }=\frac{1+1.5 \pi}{\omega_{R}}=\frac{0.909}{f_{R}}
$$

The maximum conversion frequency corresponds to the minimum conversion period, $T_{\text {CoNVmin }}$, which is the sum of the minimum ontime and maximum off-time:

## $T_{\text {CONVmin }}$ :

$$
t_{01}+t_{12 \min }+t_{23}=\frac{0.909+0.308}{f_{R}}=\frac{1.227}{f_{R}}
$$

The maximum conversion frequency, $f_{\text {convmax }}$ $=1 / T_{C_{C N V_{\text {min }}}}$, equals

$$
F_{C O N V \max }=\frac{1}{T_{C O N V(\min )}}=\frac{f_{R}}{1.227}
$$

The ratio of the maximum conversion frequency to that of the resonant tank frequency can be expressed as a topology coefficient, $\mathrm{K}_{\mathrm{T}}$. For this zero voltage switched Buck regulator and its derivatives, $\mathbf{K}_{\mathrm{T}_{\max }}$ equals:

$$
K_{T \max }=\frac{F_{C O N V \max }}{f_{R}}=\frac{f_{R} / 1.227}{f_{R}}=0.815
$$



Fig. 10 -- Waveforms at $F_{\text {CONV }}=K_{T} \cdot f_{R}$
In a realistic application, the output voltage of the power supply is held in regulation at $V_{o}$ which stipulates that the on-time in the power processing state, $\boldsymbol{t}_{34}$, cannot go to zero as in the example above. The volt-second product requirements of the output must be satisfied during this period, just as in any square wave converter design. Analogous to minimum duty cycle, the minimum on-time for a given design will be a function of $V_{I N}, V_{O}$ and the resonant tank frequency, $\omega_{R}$.

Although small, a specific amount of energy is transferred from the input to the output during the capacitor charging interval $t_{01}$. The voltage into the output filter section linearly decreases from $V_{I N}$ at time $t_{0}$ to zero at $t_{l}$, equal to an average value of $V_{I N} / 2$. In addition, a constant current equal to the output current $I_{o}$ was being supplied from the input source. The average energy transferred during this interval is defined as:

$$
W_{I N}=\frac{1}{2} V_{I N} I_{O} t_{01}=\frac{V_{I N} I_{O}}{2} \frac{C_{R} V_{I N}}{I_{O}}=\frac{V_{I N}^{2} C_{R}}{2}
$$

The equation can be reorganized in terms of $C_{R}$ and $\omega_{R}$ as:

$$
W_{I N}=\frac{V_{I N}^{2} I_{O \min }}{2 \omega_{R} V_{I N \max }}
$$

This minimum energy can be equated to minimum output watts by dividing it by its
conversion period where $t_{34}$ equals zero. Topology coefficient K-r will be incorporated to define the ratio of the maximum conversion frequency (minimum conversion period) to that of the resonant tank frequency, $\omega_{\boldsymbol{R}}$.

$$
\begin{gathered}
W_{I N}=P_{O} T_{C O N V} \text {, Where } T_{C O N V}=\frac{7.71}{\omega_{R}} \\
W_{I N}=P_{O_{\min }} \frac{7.71}{\omega_{R}}=\frac{V_{I N}^{2} I_{O_{\min }}}{2 \omega_{R} V_{I N \max }} \\
P_{O_{\min }}=V_{O} I_{O_{\min }}=\frac{V_{I N}^{2} I_{O_{\min }}}{2(7.71) V_{I N \max }}
\end{gathered}
$$

This demonstrates that a zero power output is unobtainable in reality. The same is true for the ability to obtain zero output voltage.
The equation can be rewritten as:

$$
V_{O \min }=\frac{V_{I N}^{2}}{2(7.71) V_{I N \max }}=\frac{0.065 V_{I N}^{2}}{V_{I N \max }}
$$

Solving for the highest minimum output voltage, the worst case for occurs when $I_{o}$ equals $I_{O_{\text {min }}}$ and $V_{I N}$ is at its maximum, $V_{I N m a x}$.

$$
\begin{gathered}
V_{O \min }=0.065 V_{I N \max } ; \approx 6.5 \% V_{I N \max } \\
P_{O_{\min }}=0.065 V_{I N \max } I_{O_{\min }} ; \approx 6.5 \% P_{I N \min }
\end{gathered}
$$

Under normal circumstances the circuit will be operating far above this minimum requirement. In most applications, the amount of power transferred during the capacitor charging interval $t_{0 I}$ can be neglected as it represents less than seven percent ( $7 \%$ ) of the minimum input power. This corresponds to less than one percent of the total input power assuming a 10:1 load range.

## ZVS Effective Duty Cycles:

A valid assumption is that a negligible amount of power is delivered to the load during the capacitor charging interval $t_{01}$. Also, no power is transferred during the resonant period from $t_{12}$. Although the switch is on during period $t_{23}$, it is only recharging the
resonant and output inductors to maintain the minimum output current, $I_{O_{\text {min }}}$. In summary, NO output power is derived from $V_{I N}$ during interval $\boldsymbol{t}_{03}$.

The power required to support $V_{O}$ at its current of $I_{\boldsymbol{O}}$ is obtained from the input source during the power transfer period $t_{34}$. Therefore, an effective "duty cycle" can be used to describe the power transfer interval $\boldsymbol{t}_{34}$ to that of the entire switching period, $t_{04}$, or $T_{\text {CONV }}$.
ZVS - Effective Duty Cycle Calculations:

$$
\begin{aligned}
& \text { "Duty Cycle" }=\frac{V_{o}}{V_{I N}}=\frac{t_{34}}{t_{04}} \\
& \text { "Duty Cycle" }=\frac{t_{34}}{t_{01}+t_{12}+t_{23}+t_{34}}
\end{aligned}
$$

And can be analyzed over line and load ranges using previous equations for each interval.

## Accommodating Losses in the Design Equations:

Equations for zero voltage switching using ideal components and circuit parameters have been generated, primarily to understand each of the intervals in addition to computer modeling purposes. The next logical progression is to modify the equations to accommodate voltage drops across the components due to series impedance, like $\boldsymbol{R}_{\boldsymbol{D S}(o n)}$, and the catch diode forward voltage drop. These two represent the most significant loss contributions in the buck regulator model. Later, the same equations will be adapted for the buck derived topologies which incorporate a transformer in the power stage.

The procedure to modify the equations is straightforward. Wherever $V_{I N}$ appears in the equations while the switch is on it will be replaced by $V_{I N}-V_{D S(o n)}$, the latter being a function of the load current $I_{\boldsymbol{O}}$. The equations can be further adjusted to accept changes of $R_{D S(o n)}$ and $V_{F}$, etc. with the device junction temperatures. Resonant component initial tolerances, and temperature variations likewise
could optionally be evaluated.
A computer program to calculate the numerous time intervals and conversion frequencies as a function of line and load can simplify the design process, if not prove to be indispensable. Listed in the Appendix of this section is a BASIC language program which can be used to initiate the design procedure.

To summarize: When the switch is on, replace $V_{I N}$ with $\left(V_{I N}-V_{D S(o n)}\right)=\left(V_{I N}-I_{O} . R_{D S(o n)}\right)$. When the free-wheeling diode is on, replace $V_{o}$ with $\left(V_{o}+V_{F}\right)$.

$$
\begin{aligned}
& t_{01}=\frac{C_{R}\left(V_{I N}-I_{O} R_{D S(o n)}\right)}{I_{O}} \\
& t_{12}=\frac{\pi}{\omega_{R}}+\frac{1}{\omega_{R}} \arcsin \left[\frac{V_{I N}-I_{O} R_{D S(o n)}}{I_{O} Z_{R}}\right]_{I l}^{12} \\
& t_{23}=\frac{2 L_{R} I_{O}}{V_{I N}-I_{O} R_{D S(o n)}}
\end{aligned}
$$

$$
t_{34}=\frac{\left(V_{o}+V_{F}\right)\left(t_{01}+t_{12}+t_{23}\right)}{\left(V_{I N}-I_{O} R_{D S(o n)}\right)-\left(V_{o}+V_{F}\right)}
$$

$$
Z_{R}=\frac{V_{I N \max }-R_{D S(o n)} I_{O \min }}{I_{O \min }}
$$

## Transformer Coupled Circuit Equations:

The general design equations for the Buck topology also apply for its derivates; namely the forward, half-bridge, full-bridge and push-pull converters. Listed below are the modifications and circuit specifics to apply the previous equations to transformer coupled circuits.
General Transformer Coupled Circuits. Maintaining the resonant tank components on the primary side of the transformer isolation boundary is probably the most common and simplest of configurations. The design procedure begins by transforming the output voltage and current to the primary side through the turns ratio, N . The prime (') designator will be used to signify the translated variables as seen by the primary side circuitry.

$$
N=\frac{\text { Primary Turns }}{\text { Secondary Turns }}
$$

$I_{o}{ }^{\prime}=I_{O} / \mathrm{N} ; \quad V_{o}{ }^{\prime}=V_{o} \cdot \mathrm{~N} ;$ and $Z_{O^{\prime}}=Z_{o} \cdot \mathrm{~N}^{2}$
To satisfy the condition for resonance, $I_{R}<I_{o}{ }^{\prime}$

$$
I_{R} \leq I_{O}^{\cdot}=I_{O} / N ; \quad Z_{R} \leq \frac{V_{I N \max }}{I_{O_{\text {min }}^{\prime}}}=\frac{V_{I N \max } N}{I_{O}}
$$

The resonant tank component equations now become:

$$
L_{R}=\frac{Z_{R}}{\omega_{R}}=\frac{V_{I N \max } N}{I_{O_{\min }} \omega_{R}}
$$

Note: the calculated resonant inductance value does not include any series inductance, typical of the transformer leakage and wiring inductances.

$$
C_{R}=\frac{1}{Z_{R} \omega_{R}}=\frac{I_{O_{\min }}}{N V_{I N \max } \omega_{R}}
$$

Note: the calculated resonant capacitor value does not include any parallel capacitance, typical of a MOSFET output capacitance, $C_{\text {oss }}$, in shunt. Multi-transistor variations of the buck topology should accommodate all switch capacitances in the analysis.
Timing Equations (including N):

$$
\begin{aligned}
& t_{01}=\frac{C_{R} V_{I N} N}{I_{O}} \\
& t_{12}=\frac{\pi}{\omega_{R}}+\frac{1}{\omega_{R}} \arcsin \left[\frac{V_{I N} N}{I_{O} Z_{R}}\right]_{11}^{12} \\
& t_{23}=\frac{2 L_{R} I_{O}}{V_{I N} N} \\
& t_{34}=\frac{N V_{o}\left(t_{01}+t_{12}+t_{23}\right)}{V_{I N}-N V_{O}} \\
& T_{C O N V}=t_{01}+t_{12}+t_{23}+t_{34}
\end{aligned}
$$

Determining Transformer Turns Ratio (N): The transformer turns ratio is derived from the equations used to define the power transfer interval $t_{34}$ in addition to the maximum offtime, $\boldsymbol{t}_{03}$. While this may first seem like an iterative process, it simplifies to the volt-second product relationship described. The general equations are listed below.

The turns ratio N is derived by substituting $\mathrm{N} \cdot V_{o}$ for the output voltage $V_{o}$ in the power transfer interval $t_{34}$ equation. Solving for N results in the relationship:

$$
\begin{aligned}
N V_{o} / V_{I N} & =t_{34} /\left(t_{01}+t_{12}+t_{23}+t_{34}\right) \\
N & =\frac{V_{I N \text { min }} t_{34}}{V_{o} t_{04}}
\end{aligned}
$$

The transformer magnetizing and leakage inductance is part of the resonant inductance. This requires adjustment of the resonant inductor value, or both the resonant tank impedance $Z_{R}$ and frequency $\omega_{R}$ will be off-target. One


Fig. 11 -- Transformer Inductance "Shim"
option is to design the transformer inductance to be exactly the required resonant inductance, thus eliminating one component. For precision applications, the transformer inductance should be made slightly smaller than required, and "shimmed" up with a small inductor.

## Expanding ZVS to Other Topologies

ZVS Forward Converter - Single Ended:
The single ended forward converter can easily be configured for zero voltage switching with the addition of a resonant capacitor across the switch. Like the buck regulator, there is a high voltage excursion in the off state due to resonance, the amplitude of which varies with line and load. The transformer can be designed so that its magnetizing and leakage inductance equals the required resonant inductance. This simplifies transformer reset and eliminates one component. A general circuit diagram is shown in Fig. 12 below. The associated waveforms for when $L_{P R I}$ equals $L_{R}$ are shown in Fig. 13.


Fig. 12 -- ZVS Forward Converter


## APPLICATION NOTE

ZVS Clamped Configurations -- Half and Full Bridge Topologies: Zero voltage switching can be extended to multiple switch topologies for higher power levels, specifically the half and full bridge configurations. While the basic operation of each time interval remains similar, there is a difference in the resonant $t_{12}$ interval.

While single switch converters have high offstate voltage, the bridge circuits clamp the switch peak voltages to the DC input rails, reducing the switch voltage stress. This alters the duration of the off segment of the resonant interval, since the opposite switch(es) must be activated long before the resonant cycle is completed. In fact, the opposite switch(es) should be turned on immediately after their voltage is clamped to the rails, where their drain to source voltage equals zero. If not, the resonant tank will continue to ring and return the switch voltage to its starting point, the opposite rail. Additionally, this off period varies with line and load changes.

Examples of this are demonstrated in Figs. 14 and 15. To guarantee true zero voltage switching, it is recommended that the necessary sense circuitry be incorporated.


Fig. 14 -- Clamped ZVS Configuration


Fig. 15 -- Clamped ZVS Waveforms

ZVS Half Bridge: The same turns ratio, N , relationship applies to the half bridge topology when $V_{\text {IN }}$ in the previous equations is considered to be one-half of the bulk rail-torail voltage. $V_{I N}$ is the voltage across the transformer primary when either switch is on.

Refer to the circuit and waveforms of Figs. 14 and 15. $C_{R}$, the resonant capacitor becomes the parallel combination of the two resonant capacitors, the ones across each switch. Although the resonant inductor value is unaffected, all series leakage and wiring inductance must be taken into account.

The off state voltages of the switches will try to exceed the input bulk voltage during the resonant stages. Automatic clamping to the input bulk rails occurs by the MOSFET body diode, which can be externally shunted with a higher performance variety. Unlike the forward converter which requires a core reset equal to the applied volt second product, the bidirectional switching of the half (and full) bridge topology facilitate automatic core reset during consecutive switching cycles [11,12].


Fig. 16 -- ZVS Half Bridge Circuit


Fig. 17 -- ZVS Half Bridge Wavefoms

ZVS Full Bridge: The equations represented for the forward topology apply equally well for one conversion cycle of the full bridge topology, including the transformer turns ratio. Since the resonant capacitors located at each switch are "in-circuit" at all times, the values should be adjusted accordingly. As with the half bridge converter, the resonant capacitors' voltage will exceed the bulk rails, and clamping via the FET body diodes or external diodes to the rails is common [13].


Fig. 18 -- ZVS Full Bridge Circuit


Fig. 19 -- ZVS Full Bridge Wavefoms

## ZVS Design Procedure

## Buck Derived Topologies -- Continuous output Current:

1. List all input/output specs and ranges.
$V_{I N} \min \& \max ; \mathrm{V} 0 ; I_{O} \min \& \max$
2. Estimate the maximum switch voltages. For unclamped applications (buck and forward):

$$
V_{D S \text { max }}=V_{I N \max }\left(1+\left(I_{O_{\max }} / I_{O_{\text {min }}}\right)\right.
$$

Note: Increase $I_{O_{\text {min }}}$ if $V_{D S \text { max }}$ is too high if possible).
For clamped applications (bridges): $V_{D S \text { max }}=V_{I N \text { max }}$
3. Select a resonant tank frequency, $\omega_{R}$ (HINT: $\omega_{R}=2 \pi f_{R}$ ).
4. Calculate the resonant tank impedance and component values.
5. Calculate each of the interval durations ( $t_{01}$ thru $\boldsymbol{t}_{34}$ ) and their ranges as a function of all line and load combinations.
(See Appendix for a sample computer program written in BASIC)
Additionally, summarize the results to establish the range of conversion frequencies, peak voltages and currents, etc.
6. Analyze the results. Determine if the frequency range is suitable for the application. If not, a recommendation is to limit the load range by raising $I_{O_{\text {min }}}$ and start the design procedure again. Verify also that the design is feasible with existing technology and components.
7. Finalize the circuit specifics and details.

- Derive the transformer turns ratio. (nonbuck applications)
$\square$ Design the output filter section based upon the lowest conversion frequency and output ripple current, $I_{0}(\mathrm{ac})$.
$\square$ Select applicable components; diode, MOSFET etc.

8. Breadboard the circuit carefully using RF techniques wherever possible. Remember -parasitic inductances and capacitances prefer to resonate upon stimulation, and quite often, unfavorably.
9. Debug and modify the circuit as required to accommodate component parasitics, layout concerns or packaging considerations.

## Avoiding Parasitics

Ringing of the catch diode junction capacitance with circuit inductance (and package leads) will significantly degrade the circuit performance. Probably the most common solution to this everyday occurrance in square wave converters is to shunt the diode with an R-C snubber. Although somewhat dissipative, a compromise can be established between snubber losses and parasitic overshoot caused by the ringing. Unsnubbed examples of various applicable diodes are shown in Fig. 20 below.


Fig. 20 -- Catch Diode Ringing

## Multiresonant ZVS Conversion

Another technique to avoid the parasitic resonance involving the catch diode capacitance is to shunt it with a capacitor much larger than the junction capacitance. Labelled $C_{D}$, this element introduces favorable switching characteristics for both the switch and catch diode. The general circuit diagram and associated waveforms are shown below, but will not be explored further in this presentation [14,15].


Fig. 21 -- Multiresonant ZVS Circuit

## Current Mode Controlled

ZVS Conversion
Variable frequency power converters can also benefit from the use of current mode control. Two loops are used to determine the precise ON time of the power switch -- an "outer" voltage feedback loop, and an "inner" current sensing loop. The advantage to this approach is making the power stage operate as a voltage controlled current source. This eliminates the two pole output inductor characteristics in addition to providing enhanced dynamic transient response.

Principles of operation. Two control ICs are utilized in this design example. The UC3843A PWM performs the current mode control by providing an output pulse width determined by the two control loop inputs. This pulse width, or repetition rate is used to set the conversion period of the UC3864 ZVS resonant controller. Rather than utilize its voltage controlled oscillator to generate the conversion period, it is


Fig. 22 -- Multiresonant Waveforms
determined by the UC3843A output pulse width.

Zero voltage switching is performed by the UC3864 one-shot timer and zero crossing detection circuitry. When the resonant capacitor voltage crosses zero, the UC3864 output goes high. This turns ON the power switch and recycles the UC3843A to initiate the next current mode controlled period. The UC3864 fault circuitry functions, but its error amplifier and VCO are not used.

## ZVS Forward Converter -- Design Example

1. List circuit specifications:

$$
\begin{aligned}
& V_{I N}=18 \text { to } 26 \mathrm{~V} \\
& V_{O}=5.0 \mathrm{~V} ; \quad I_{O}=2.5 \text { to } 10 \mathrm{~A}
\end{aligned}
$$

2. Estimate the maximum voltage across the switch:

$$
\begin{aligned}
& V_{D S \text { max }}=V_{I N \text { max }}\left(1+\left(I_{\left.O_{\max } / I I_{\text {min }}\right)}\right.\right. \\
& =26 \bullet(1+(10 / 2.5))=26 \cdot 5=130 \mathrm{~V}
\end{aligned}
$$

## 3. Select a resonant tank frequency, $\omega_{\mathbf{R}}$.

A resonant tank period frequency of 500 KHz will be used. It was selected as a compromise between high frequency operation and low parasitic effects of the components and layout.
$f_{R}=500 \mathrm{KHz} ; \omega_{\mathrm{R}}=3.14 \cdot 10^{6}$ radians $/ \mathrm{sec}$
4. Calculate the resonant tank impedance and component values.
Resonant tank impedance, $Z_{R}>V_{I N \text { max }} / I_{O_{\text {min }}}$ To accommodate the voltage drop across the MOSFET, calculate $V_{D S(o n) m i n}$, which equals $R_{D S(\text { on })} I_{\text {Omin }}=0.8 \cdot 2.5=2 \mathrm{~V}$
$Z_{R}=\left(V_{I N \text { max }}-V_{D S \text { min }}\right) / I_{O_{\text {min }}}$
$Z_{R}=(26-2) / 2.5=10 \Omega$
$C_{R}=1 /\left(Z_{R} \omega_{\mathrm{R}}\right)=1 /\left(10 \cdot 3.14 \cdot 10^{6}\right)=32 \mathrm{nF}$
$L_{R}=Z_{R} / \omega_{\mathrm{R}}=10 / 3.34 \cdot 10^{6}=3.18 \mu \mathrm{H}$
5. Calculate each of the interval durations ( $t_{o t}$ thru $t_{30}$ ) and ranges as they vary with line and load changes.

The zero voltage switched buck converter "gain" in kiloHertz per volt of $V_{I N}$ and kHz per amp of $I_{O}$ can be evaluated over the specified ranges. A summary of these follows:

Table VI - Interval Durations vs. Line \& Load

|  | $\begin{aligned} & V_{V_{N}}=18 \\ & I_{O}=2.5 \end{aligned}$ | $\begin{aligned} & V_{I N}=18 \\ & I_{0}=10 \end{aligned}$ | $\begin{aligned} & V_{I N}=26 \\ & I_{0}=2.5 \end{aligned}$ | $\begin{aligned} & V_{I N}=26 \\ & I_{0}=10 \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |
| $t_{10}$ | 0.217 | 0.055 | 0.314 | 0.078 |
| $\mathrm{t}_{12}$ | 1.29 | 1.06 | 1.49 | 1.08 |
| ${ }^{12}$ | 0.93 | 3.72 | 0.64 | 2.58 |
| ${ }^{1}$ | 1.39 | 6.68 | 0.78 | 1.78 |
| TCONV | 3.83 | 11.51 | 3.23 | 5.52 |
| ${ }^{\text {f Conv }}$ | 261 kHz | 87kHz | 310kHz | 181kHz |
| Transistor Switch Durations: |  |  |  |  |
| \% | 2.32 | 10.4 | 1.42 | 4.36 |
| toff | 1.51 | 1.11 | 1.80 | 1.16 |



Fig. 23-Switch Times vs. Line \& Load

\[

\]

Highest "gain" ( $11.9 \mathrm{kHz} / \mathrm{V}$ ) occurs near full load.

\[

\]

Highest "gain" $(23.3 \mathrm{kHz} / \mathrm{A})$ occurs at $V_{\text {IN min }}$.
It may be necessary to use the highest gain values to design the control loop compensation for stability over all operating conditions. While this may not optimize the loop transient response for all operating loads, it will guarantee stability over the extremes of line and load.


Fig. 24 - Conversion Freq. vs. Line \& Load

## 6. A nalyze the results.

The resonant component values, range of conversion frequencies, peak voltage and current ratings seem well within the practical limits of existing components and technology.
7. Finalize the circuit specifics and details based on the information obtained above.
A. Output Filter Section: Select $L_{o}$ and $C_{o}$ for operation at the lowest conversion frequency and designed ripple current.
B. Heatsink Requirements: An estimate of the worst case power dissipation of the power switch and output catch diode can be made over line and load ranges.
C. Control Circuit: The UC3861-64 series of controllers will be examined and programmed per the design requirements.

## Programming the Control Circuit

0 ne-shot= Accommodating 0 ff-time V ariations. The switch off-time varies with line and load by $\approx \pm 35 \%$ in this design example using ideal components. Accounting for initial tolerances and temperature effects results in an much wider excursion. For all practical purposes, a true fixed off-time technique will not work.

Incorporated into the UC3861 family of ZVS controllers is the ability to modulate this off-


Fig. 25 -- The UC 3861-64 ZVS Controllers -- Block Diagram


Fig. 26 -- $\boldsymbol{C}_{\boldsymbol{R}}$ Volts \& Off-time vs. Line \& Load
time. Initially, the one-shot is programmed for the maximum off-time, and modulated via the ZERO detection circuitry. The switch drainsource voltage is sensed and scaled to initiate turn-on when the precision 0.5 V threshold is crossed. This offset was selected to accommodate propogation delays between the instant the threshold is sensed and the instant that the switch is actually turned on. Although brief, these delays can become significant in high frequency applications, and if left unaccounted, can cause NONZERO switching transitions.

Referring to Fig. 26, in this design, the offtime varies between 1.11 and 1.80 microseconds, using ideal components and neglecting temperature effects on the resonant components. Since the ZERO detect logic will facilitate "true" zero voltage switching, the off-time can be set for a much greater period. The one-shot has a $3: 1$ range capability and will be programmed for 2.2 us (max), controllable down to 0.75 uS. Programming of the one-shot require a single R-C time constant, and is straightforward using the design information and equations from the data sheet. Implementation of this feature is shown in the control circuit schematic.

Programming the VCO. The calcu-
lated range of conversion frequencies spans 87 to 310 kHz . These values will be used for this "first cut" draft of the control circuit programming. Due to the numerous circuit specifics omitted from the computer program for simplicity, the actual range of conversion frequencies will probably be somewhat wider than planned. Later, the actual timing component values can be adjusted to accommodate these differences.

First, a minimum $f_{C}$ of 75 kHz has been selected and programmed according to the following equation:

$$
F_{v c o \min }=3.6 /\left(R_{\min } C_{v c o}\right)
$$

The maximum $f_{C}$ of 350 kHZ is programmed by:

$$
F_{V C O \max }=3.6 /\left(R_{\min } \| R_{\text {range }}\right) \cdot C_{V C O}
$$

Numerous values of $R_{\min }$ and $C_{V C O}$ will satisfy the equations. The procedure can be simplified by letting $\boldsymbol{R}_{\text {min }}$ equal 100 K .

$$
C_{Y C O}(\mu \mathrm{~F})=0.036 / f_{\min }(\mathrm{kHz})
$$

$R_{\text {RANGE }}(\mathrm{k} \Omega)=100 /\left(f_{\text {CONVmax }} / f_{\text {CONVmin }}-1\right)$
where $R_{\text {min }}=100 \mathrm{~K}, C_{V C O}=470 \mathrm{pF}, R_{\text {RANGE }}=27 \mathrm{~K}$
The VCO gain in frequency per volt from the error amplifier output is approximated by:

$$
d F / d V=1 /\left(R_{R A N G E} C_{V C O}\right)=78.2 \mathrm{kHz} / \mathrm{V}
$$

with an approximate 3.6 volt delta from the error amplifier.

VOLTAGE CONTROLLED OSCILLATOR
E/a


Fig. 27 -- E/A - VCO Block Diagram

Fault Protection - Soft Start \& Restart Delay One of the unique features of the UC 3861 family of resonant mode controllers can be found in its fault management circuitry. A single pin connection interfaces with the soft start, restart delay and programmable fault mode protection circuits. In most applications, one capacitor to ground will provide full protection upon power-up and during overload conditions. Users can reprogram the timing relationships or add control features (latch off following fault, etc) with a single resistor.

Selected for this application is a 1 uF softrestart capacitor value, resulting in a soft-start duration of 10 ms and a restart delay of approximately 200 ms . The preprogrammed ratio of 19:I (restart delay to soft start) will be utilized, however the relevant equations and relationships have also been provided for other applications. Primary current will be utilized as the fault trip mechanism, indicative of an overload or short circuit current condition. A current transformer is incorporated to maximize efficiency when interfacing to the three volt fault threshold.

Optional Programming of $T_{S S}$ and $T_{R D}$ :

$$
\begin{aligned}
& \text { Soft Start: } T_{S S}=C_{S R} \bullet 10 \mathrm{~K} \\
& \text { Restart Delay: } \boldsymbol{T}_{\boldsymbol{R}}=C_{\boldsymbol{S}} \bullet 190 \mathrm{~K} \\
& \text { Timing Ratio: } \boldsymbol{T}_{\boldsymbol{R}}: \boldsymbol{T}_{\boldsymbol{S S}}=19: 1
\end{aligned}
$$

Gate Drive: Another unique feature of the UC 3861-64 family of devices is the optimal utilization of the silicon devoted to output totem pole drivers. Each controller uses two pins for the A and B outputs which are internally configured to operate in either unison or in an alternating configuration. Typical performance for these 1 Amp peak totem pole outputs shows 30 ns rise and fall times into $\mathbf{1 n F}$.

Loop Compensation -- General Information. The ZVS technique is similar to that of conventional voltage mode square wave conversion which utilizes a single voltage feedback loop. Unlike the dual loop system of current mode control, the ZVS output filter section exhibits


Fig. 28 -- Programming $\mathbf{T}_{\mathbf{S S}}$ and $\mathbf{T}_{\mathbf{R D}}$


Fig. 29 -- Fault Operational Waveforms
a two pole-zero pair and is compensated accordingly. Generally, the overall loop is designed to cross zero dB at a frequency below one-tenth that of the switching frequency. In this variable frequency converter, the lowest conversion frequency will apply, corresponding to approximately 85 KHz , for a zero crossing of 8.5 KHz. Compensation should be optimized for the highest low frequency gain in addition to ample phase margin at crossover. Typical examples utilize two zeros in the error amplifier compensation at a frequency equal to that of the output filter's two pole break. An additional high frequency pole is placed in the loop to combat the zero due to the output capacitance ESR, assuming adequate error amplifier gainbandwidth.

A noteworthy alternative is the use of a two loop approach which is similar to current mode control, eliminating one of the output poles. One technique known as Multi-Loop Control for Quasi-Resonant Converters [18] has been
developed. Another, called Average Current Mode Control is also a suitable candidate,

$$
\begin{gathered}
\omega_{P l}=\frac{1}{R_{F P} C_{F}} ; \quad \omega_{Z 1}=\frac{1}{\left(R_{F P} \| R_{F Z}\right) C_{F}} \\
\omega_{Z Z}=\frac{1}{\left(R_{I P}+R_{I Z}\right) C_{I}} ; \quad \omega_{P 2}=\frac{1}{R_{I P} C_{I}}
\end{gathered}
$$



Fig. 30 - Error Amplifier Compensation

## Summary

The zero voltage switched quasi-resonant technique is applicable to most power conversion designs, but is most advantageous to those operating from a high voltage input. In these applications, losses associated with discharging of the MOSFET output capacitance can be significant at high switching frequencies, impairing efficiency. Zero voltage switching avoids this penalty by negating the drain-to-source, "off-state" voltage via the resonant tank.

A high peak voltage stress occurs across the switch during resonance in the buck regulator and single switch forward converters. Limiting this excursion demands limiting the useful load range of the converter as well, an unacceptable solution in certain applications. For these situations, the zero voltage switched multiresonant approach [14,15] could prove more beneficial than the quasi-resonant ZVS variety.

Significant improvements in efficiency can be obtained in high voltage, half and full bridge ZVS applications when compared to their square wave design complements. Clamping of


Fig. 31-Zero Voltage Switched Forward Converter
the peak resonant voltage to the input rails avoids the high voltage overshoot concerns of the single switch converters, while transformer reset is accomplished by the bidirectional switching. Additionally, the series transformer primary and circuit inductances can beneficial, additives in the formation of the total resonant inductor value. This not only reduces size, but incorporates the detrimental parasitic generally snubbed in square wave designs, further enhancing efficiency.

A new series of control ICs has been developed specifically for the zero voltage switching techniques with a list of features to facilitate lossless switching transitions with complete fault protection. The multitude of functions and ease of programmability greatly simplify the interface to this new generation of power conversion techniques; those developed in response to the demands for increased power density and efficiency.


Fig. 32 -- Zero Voltage Switched Half-Bridge Converter

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10' Zero Voltage Switching Calculations and Equations
20' Using the Continuous Current Buck Topology
30' in a Typical DC/DC Converter Power Supply Application
40'
50 PRINTER$ = "lptl:": ' Printer at parallel port #| **********
60
70 ' Summary of Variables and Abbreviations
80'
90' Cr = Resonant Capacitor
100 ' Lr = Resonant Inductor
110 ' Zr = Resonant Tank Impedance
120' Fres = Resonant Tank Frequency (Hz)
130'
140' VImin = Minimum DC Input Voltage
150' VImax = Maximum DC Input Voltage
160' Vdson = Mosfet On Voltage = lo*Rds
170 ' Rds = Mosfet On Resistance
180' Vdsmax = Peak MOSFET Off State Voltage
190' Vo = DC Output Voltage
200 ' Vdo = Output Diode Voltage Drop
210' Iomax = Maximum Output Current
220' Iomin = Minimum Output Current
230'
240 ' Start with parameters for low voltage dc/dc buck regulator
250'
260 ' ****Define 5 Vi and 5 lo data points ranging from min to max*****
270 ' (Suggestion: With broad ranges, use logarithmic spread)
280 DATA 18,20,22,24,27 : 'Vi data
290 DATA 2.5,4,6,8,10 : 'lo data
300 FRES = 500000!
310 VO = 5!
320 VDO = . 8
330 RDS = .8
340 SAFT = .95
350'
360 FOR J = 1 TO 5: READ VI(J): NEXT
370 FOR K = 1 TO 5: READ IO(K): NEXT
380 CLS
390 PRINT "For output to screen, enter 'S' or 'S'."
400 INPUT "Otherwise output will be sent to printer : ", K$
410 IF K$ = "S" OR K$ = "s" THEN K$ = "scrn:" ELSE K$ = PRINTER$
420 OPEN K$ FOR OUTPUT AS #1: CLS
430 PRINT #1, "================================================="
440 PRINT #1, "Zero Voltage Switching Times (uSec) vs. Vi, lo"
450 PRINT #1,"========================================================="
460 '
```

```
470
    '========HERE GOES========
480
490 VIMAX = VI(5): IOMIN = IO(1): IOMAX = IO(5)
500 ZR = (VIMAX - (RDS * IOMIN)) / (IOMIN * SAFT)
510 WR = 6.28 * FRES
520 CR = 1 / (ZR * WR)
530 LR = ZR / WR
540
550 FOR J = 1 TO 5: VI = VI(J)
560 PRINT #I, USING " Input Voltage = ###.## V"; VI
570 FOR K = 1 TO 5: IO = IO(K)
580 RSIN = (VI / (IO * ZR)): VDSON = RDS * IO
590'
600 D(0,K) = IO * .00000I: ' Compensate for later mult. by 10^6
610 D(I, K) = (CR * VI) / IO: 'dtO1
620 D(2, K) = (3.14 / WR) + (1 / WR) * ATN(RSIN / (1 - RSIN ^ 2)): `dt12
630 D(3, K) = (2 * LR * IO) / VI: 'dt23
640 D(6,K) = D(1, K) + D(2,K) + D(3, K): ' dt03
650 D(4, K) = ((VO + VDO) * D(6, K)) / ((VI - VDSON) - (VO + VDO)): 'dt34
660 D(5,K) = D(1 K) + D(2,K) + D(3,K) + D(4, K): 'Tconv
670 NEXT K
680
690 PAR$(0) = "lo (A) ="
700 PAR$(I) = "dt01 ="
710 PAR$(2) = "dt12 ="
720 PAR$(3) = "dt23 ="
730 PAR$(4) = "dt34 ="
740 PAR$(5) = "Tconv ="
750 PAR$(6) = "dt03 ="
760
770 FOR P = 0 TO 6
780 PRINT #1, PAR$(P);
790 FOR K = 1 TO 5
800 PRINT #I, USING " ####.###"; D(P, K) * I000000!;
810 NEXT K: PRINT #I,
8 2 0 ~ N E X T ~ P ~
830 PRINT #I,
8 4 0 ~ N E X T ~ J ~
850
860 PRINT #I, "Additional Information:"
870 PRINT #I, "Zr(Ohms) ="; INT(IOOO! * ZR) / 1000
880 PRINT #I, "wR(KRads)="; INT(WR / 1000)
890 PRINT #l. "Cr(nF) ="; INT((IO00 * CR) / 10 ^ -9) / 1000
900 PRINT #I, "Lr(uH) ="; INT((1000 * LR) / 10 ^ -6) / 1000
910 PRINT #I, "Vdsmax ="; VIMAX * (1 + IOMAX / IOMIN)
920 END
```

| Input Voltage $=18.00 \mathrm{~V}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Io (A) = | 2.500 | 4.000 | 6.000 | 8.000 | 10.000 |
| dt01 | 0.218 | 0.136 | 0.091 | 0.068 | 0.054 |
| dt12 = | 1.290 | 1.153 | 1.096 | 1.070 | 1.056 |
| dt23 | 0.931 | 1.490 | 2.235 | 2.980 | 3.725 |
| dt34 = | 1.387 | 1.791 | 2.682 | 4.118 | 6.677 |
| Tconv = | 3.825 | 4.571 | 6.103 | 8.236 | 11.511 |
| dt03 | 2.439 | 2.780 | 3.421 | 4.118 | 4.835 |
| Input Voltage $=20.00 \mathrm{~V}$ |  |  |  |  |  |
| Io (A) = | 2.500 | 4.000 | 6.000 | 8.000 | 10.000 |
| dt01 = | 0.242 | 0.151 | 0.101 | 0.076 | 0.061 |
| dt12 | 1.339 | 1.175 | 1.108 | 1.079 | 1.062 |
| dt23 | 0.838 | 1.341 | 2.011 | 2.682 | 3.352 |
| dt34 | 1.150 | 1.406 | 1.987 | 2.852 | 4.186 |
| Tconv | 3.569 | 4.074 | 5.207 | 6.688 | 8.661 |
| $\mathrm{dt03}$ | 2.419 | 2.667 | 3.220 | 3.836 | 4.475 |
| Input Voltage $=22.00 \mathrm{~V}$ |  |  |  |  |  |
| Io (A) = | 2.500 | 4.000 | 6.000 | 8.000 | 10.000 |
| dt $01=$ | 0.266 | 0.166 | 0.111 | 0.083 | 0.067 |
| dt12 | 1.390 | 1.198 | 1.120 | 1.087 | 1.069 |
| dt23 | 0.762 | 1.219 | 1.829 | 2.438 | 3.048 |
| dt34 | 0.988 | 1.153 | 1.557 | 2.136 | 2.958 |
| Tconv | 3.406 | 3.737 | 4.616 | 5.744 | 7.141 |
| dt03 = | 2.418 | 2.584 | 3.060 | 3.608 | 4.183 |
| Input Voltage $=24.00 \mathrm{~V}$ |  |  |  |  |  |
| lo (A) = | 2.500 | 4.000 | 6.000 | 8.000 | 10.000 |
| $\mathrm{dt01}$ | 0.290 | 0.182 | 0.121 | 0.091 | 0.073 |
| dt12 | 1.442 | 1.223 | 1.133 | 1.096 | 1.075 |
| dt23 | 0.698 | 1.117 | 1.676 | 2.235 | 2.794 |
| dt34 | 0.870 | 0.975 | 1.268 | 1.682 | 2.241 |
| Tconv | 3.301 | 3.498 | 4.199 | 5.103 | 6.183 |
| dt03 | 2.431 | 2.522 | 2.930 | 3.421 | 3.941 |
| Input Voltage $=27.00 \mathrm{~V}$ |  |  |  |  |  |
| Io (A) = | 2.500 | 4.000 | 6.000 | 8.000 | 10.000 |
| dt01 | 0.327 | 0.204 | 0.136 | 0.102 | 0.082 |
| dt12 | 0.516 | 1.264 | 1.153 | 1.109 | 1.085 |
| dt23 | 0.621 | 0.993 | 1.490 | 1.987 | 2.483 |
| dt34 | 0.442 | 0.793 | 0.983 | 1.253 | 1.604 |
| Tconv | 1.906 | 3.254 | 3.763 | 4.451 | 5.254 |
| dt03 | 1.464 | 2.461 | 2.780 | 3.198 | 3.650 |

Additional Information:
$\mathrm{Zr}($ Ohms $)=10.526$
$w R($ KRads $)=3140$
$\mathrm{Cr}(\mathrm{nF})=30.254$
$\operatorname{Lr}(\mathrm{uH})=3.352$
Vdsmax $=135$

